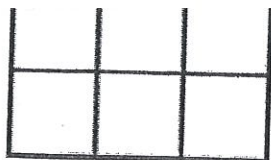


2



$2 \times 3 = 6$

There is six part in the rectangle

b. What fraction of the area of each rectangle is shaded? ways as you can. Explain your answers.

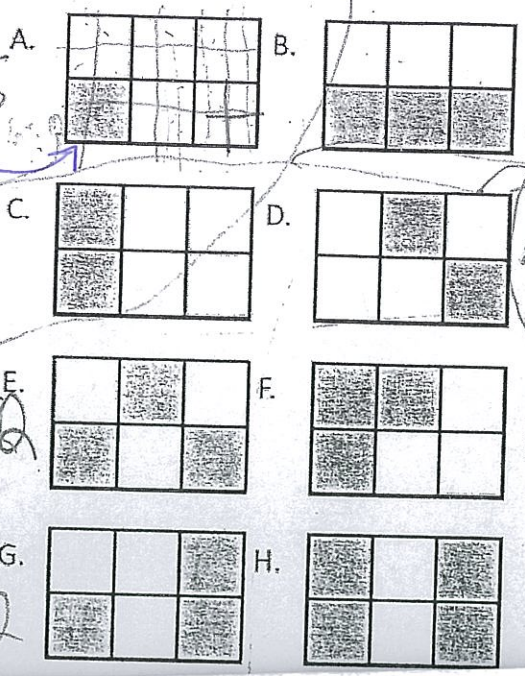
Name the fraction in as many

Handwritten notes on the left side of the page, including various fractions and calculations:

$\frac{8}{15}$, $\frac{4}{12}$, $\frac{2}{12}$, $\frac{1}{6}$

$\frac{8}{15}$, $\frac{8}{15}$, $\frac{4}{12}$, $\frac{2}{12}$, $\frac{1}{6}$, $\frac{1}{3}$

$\frac{1}{2}$






Handwritten notes on the right side of the page:

You can't partition because you can't partition into 4 equal parts. $\frac{1}{6}$ $\frac{4}{12}$ $\frac{1}{3}$ $\frac{2}{6}$ $\frac{1}{3}$

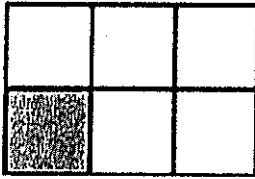
$\frac{2}{3}$ $\frac{9}{6}$ $\frac{8}{12}$ $\frac{16}{24}$

Student:

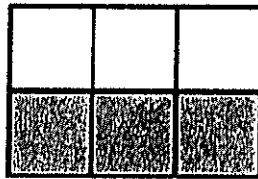
" I took the array in letter A  which is $\frac{1}{6}$, and broke it into 12 smaller equal parts -  which shows that $\frac{1}{6}$ and $\frac{2}{12}$ take up the same part of the whole. I can divide it into ~~12~~ ²⁴ equal parts  and now it shows that $\frac{1}{6} = \frac{2}{12}$ which is also equal to $\frac{4}{24}$. I noticed a pattern. Each step the numerator doubles + the denominator doubles. "

1/6

A.

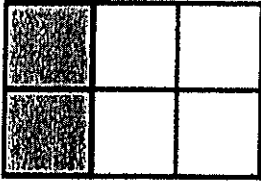


B.

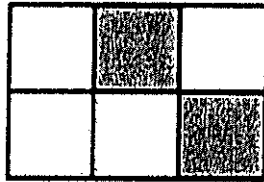


$$\frac{2}{6}$$

C.



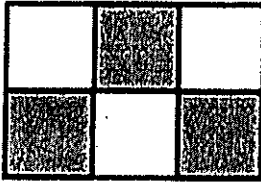
D.



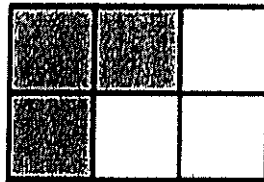
$$\frac{2}{6}$$

$$\frac{4}{6}$$

E.

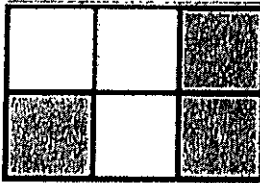


F.

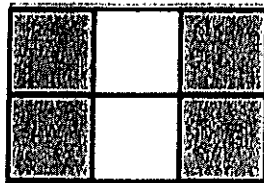


$$\frac{3}{6}$$

G.



H.



$$\frac{4}{6}$$

$$\frac{2}{6}$$

4 parts
are blue

$$\frac{4}{6}$$

$$\frac{2}{6}$$

$$\frac{3}{6}$$

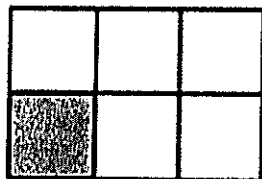
$$\frac{3}{6}$$

8

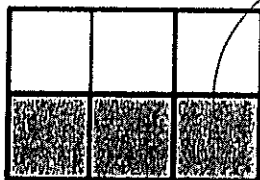
$$3 \div 3 = 1$$

$$6 \div 3 = 2$$

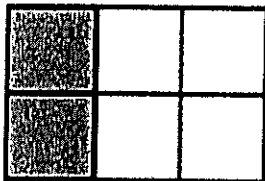
A.



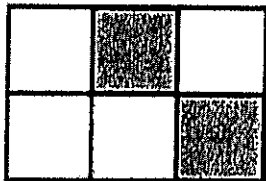
B.



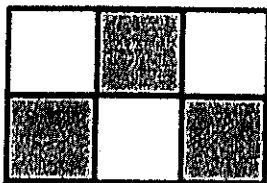
C.



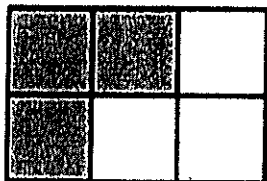
D.



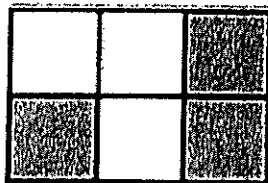
E.



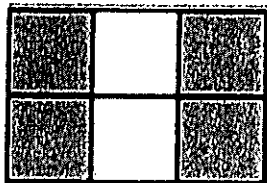
F.



G.



H.



$$6 \div 1 = 6$$

$$6 \div 2 = 3$$

$$6 \div 3 = 2$$

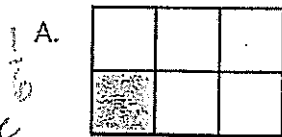
$$6 \div 2 = 3$$

$$2 \div 3 = \frac{2}{3}$$

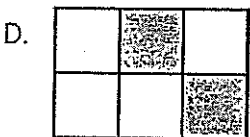
$$\frac{1}{2} \div 3 = \frac{1}{6}$$

$$\frac{3}{6} \div 2 = \frac{1}{4}$$

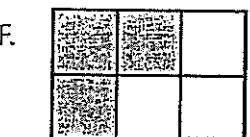
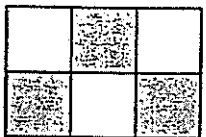
What fraction of the area of each rectangle is shaded? Name the fraction in as many ways as you can. Explain your answers. Gr 3 - Student 4



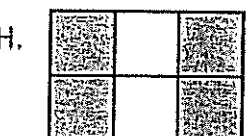
$\frac{1}{3}$ or $\frac{1}{6}$ because 3 out of 6 is shaded or 1 out of 6



$\frac{2}{6}$ or $\frac{1}{3}$ because 2 out of 6 is shaded and because 2 is a half of 6



$\frac{3}{6}$ or $\frac{1}{2}$ because 3 out of 6 is shaded and 3 is half of 6



$\frac{4}{6}$ or $\frac{2}{3}$ because 4 out of 6 is shaded and 4 is 2/3 of 6

because 1 out of 6 is shaded

$\frac{2}{6}$ or $\frac{1}{3}$ because 2 out of 6 is shaded

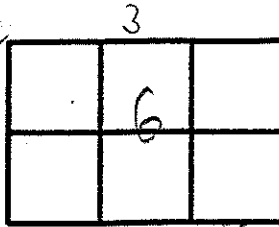
because 3 out of 6 is shaded or 1/2 of 6

made $\frac{1}{2}$ of the area of rectangle in a way that is different from the rectangles above.



a. A small square is a square unit. What is the area of this rectangle? Explain.

If you multiply
 3×2 you will get
 the area. if you
 multiply 2 and 2
 and 2 and 3 you will get



$$\begin{array}{r} 2 \\ \times 3 \\ \hline 6 \end{array}$$

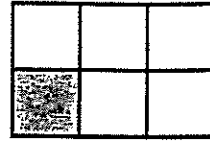
Gr 4
 Student 1
 (p 1 of 2)

b. What fraction of the area of each rectangle is shaded blue? Name the fraction in as many ways as you can. Explain your answers.

perimeter,

$\frac{1}{6}$

A.



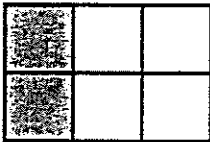
B.



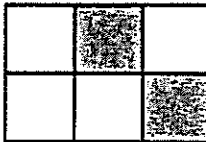
$\frac{1}{2}$

$\frac{2}{6}$

C.



D.



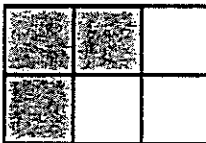
$\frac{2}{6}$

$\frac{1}{2}$

E.



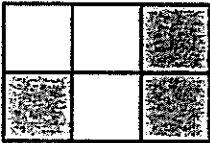
F.



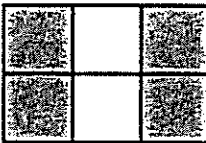
$\frac{1}{2}$

$\frac{1}{2}$

G.

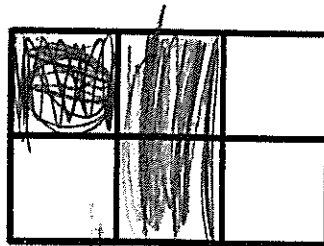


H.

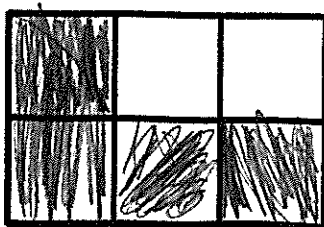


$\frac{4}{6}$

c. Shade $\frac{1}{2}$ of the area of rectangle in a way that is different from the rectangles above.



d. Shade $\frac{2}{3}$ of the area of the rectangle in a way that is different from the rectangles above.



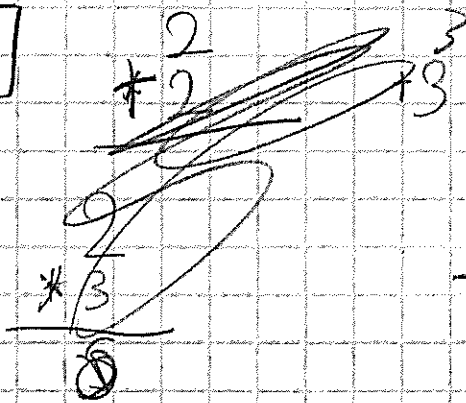
6/12/15

Gr 4

Student 1

(p 2 of 2)

a.



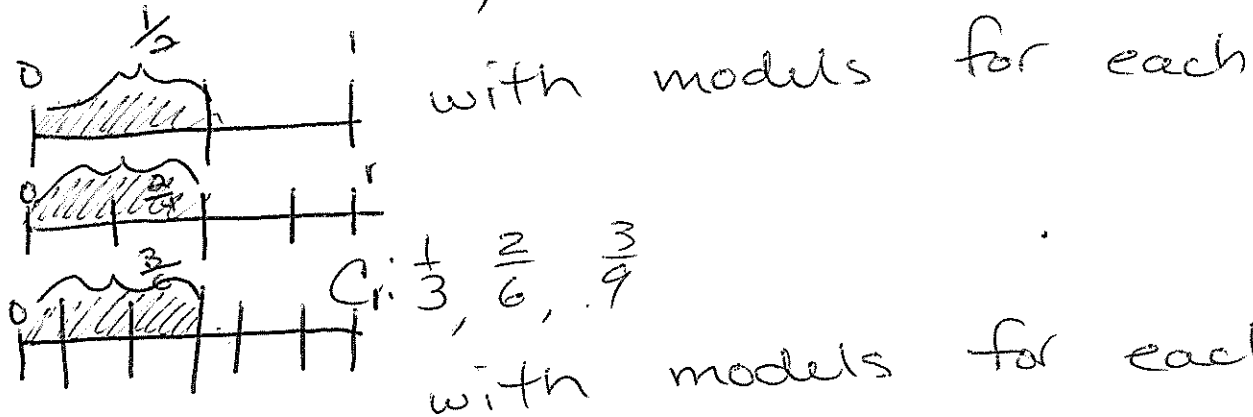
$$\begin{array}{r} 2 \\ \times 3 \\ \hline 6 \end{array}$$

b. for the fraction A-H you would
the part I shaded in ex A it's
1 only one is shaded in and
6 you would count the rest.

A: $\frac{1}{6}, \frac{2}{12}, \frac{3}{8}$

Gr 4
Student 2

B: $\frac{1}{2}, \frac{2}{4}, \frac{3}{6}$

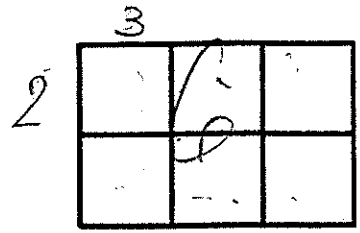


I know these fractions are equivalent because the shaded ~~part~~ area for each equivalent fraction is the same (amount).

> models demonstrate understanding of comparison of equivalent wholes. Clearly labeled models

a. A small square is a square unit. What is the area of this rectangle? Explain.

4 sq
3



Gr 4-
Student 3
(1 of 2)

b. What fraction of the area of each rectangle is shaded blue? Name the fraction in as many ways as you can. Explain your answers.

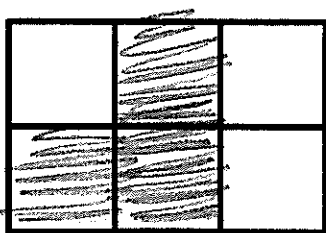
A. B.

C. D.

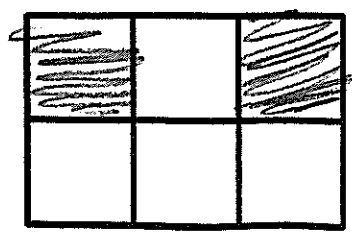
E. F.

G. H.

c. Shade $\frac{1}{2}$ of the area of rectangle in a way that is different from the rectangles above.



d. Shade $\frac{2}{3}$ of the area of the rectangle in a way that is different from the rectangles above.



Q. $2 \times 3 = 6$. The formula for area is $L \times W = A$

A. $\frac{1}{6}, \frac{2}{12}, \frac{4}{24}, \frac{8}{48}, \frac{16}{96}, \frac{32}{192}, \frac{64}{384}, \frac{128}{768}, \frac{256}{1536}$ each time I make the fraction smaller, but all of the fractions listed above are equal

B. $\frac{1}{2}, \frac{2}{4}, \frac{3}{6}, \frac{4}{8}, \frac{5}{10}, \frac{6}{12}, \frac{7}{14}, \frac{8}{16}, \frac{9}{18}, \frac{10}{20}, \frac{11}{22}, \frac{12}{24}, \frac{13}{26}, \frac{14}{28}, \frac{15}{30}, \frac{16}{32}, \frac{17}{34}$
 $\frac{18}{36}$ (I can keep going but that would take a while.)
 All of these fractions are equal because they are halves.

C. $\frac{1}{3}, \frac{2}{6}, \frac{3}{12}, \frac{4}{24}, \frac{5}{48}, \frac{6}{96}, \frac{7}{192}, \frac{8}{384}, \frac{9}{768}, \frac{10}{1536}$ all of these are equal, and they all can be reduced to thirds (except for the $\frac{1}{3}$).

D. $\frac{1}{3}, \frac{2}{6}, \frac{4}{12}, \frac{8}{24}, \frac{16}{48}, \frac{32}{96}, \frac{64}{192}, \frac{128}{384}, \frac{256}{768}, \frac{512}{1536}$ These are all equal and can be reduced to $\frac{1}{3}$ (except for the $\frac{1}{3}$).

E. $\frac{1}{2} = \frac{18}{36}$ all of the fractions are halves.

F. $\frac{1}{2} = \frac{18}{36}$ all of the fractions are halves.

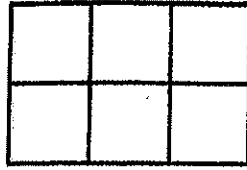
G. $\frac{1}{2} = \frac{18}{36}$ all of the fractions are equal because they are halves.

H. $\frac{4}{6}, \frac{8}{12}, \frac{16}{24}, \frac{32}{48}, \frac{64}{96}, \frac{128}{192}$ all of these fractions are equal because if reduced, all can come to $\frac{2}{3}$.

$\frac{2}{3}$

a. A small square is a square unit. What is the area of this rectangle? Explain.

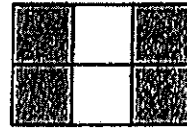
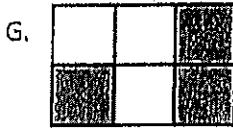
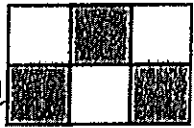
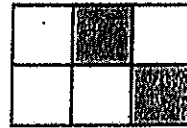
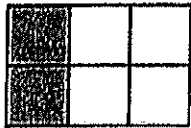
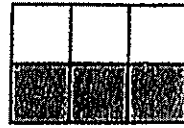
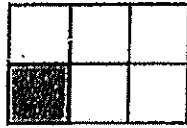
To get the area you multiply length \times width.
 $(2) \times (3)$
 I got 6^2 units



2^2 units \times 3^2 units = 6 sq. units

b. What fraction of the area of each rectangle is shaded blue? Name the fraction in as many ways as you can. Explain your answers.

$A = \frac{1}{6} = \frac{2}{12} = \frac{4}{24} = \frac{8}{48} = \frac{16}{96} = \frac{32}{192}$
 $B = \frac{1}{2}$ same as E, F, G
 $C = \frac{1}{3} = \frac{2}{6} = \frac{4}{12} = \frac{8}{24} = \frac{16}{48} = \frac{32}{96}$
 $D = \frac{1}{3}$ same as C
 $E = \frac{1}{2}$ same as F and G
 $F = \frac{1}{2} = \frac{3}{6} = \frac{4}{8} = \frac{6}{12} = \frac{8}{16} = \frac{10}{20}$
 $H = \frac{2}{3} = \frac{4}{6} = \frac{8}{12} = \frac{16}{24} = \frac{32}{48} = \frac{64}{96}$

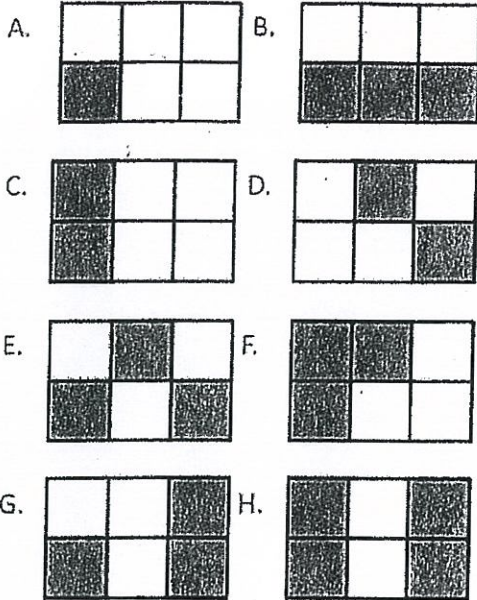


I got all the equivalent fractions because I multiplied all the fractions by $\frac{2}{2}$. To get my first solution by taking the one unit which was 6 boxes and counted all the colored boxes to get $\frac{1}{6}$ which means 1 out of 6 pieces. Then I multiplied that by $\frac{2}{2}$.



6 square units
 $2^2 \text{ units} \times 3^2 \text{ units} = 6^2 \text{ uni}$
 sq

b. What fraction of the area of each rectangle is shaded ~~blue~~ gray? Name the fraction in as many ways as you can. Explain your answers.



$A = \frac{1}{6} = \frac{2}{12} = \frac{4}{24} = \frac{5}{30} = \frac{3}{18} = \frac{6}{36}$
 $B = \frac{3}{6} = \frac{1}{2}$
 $C = \frac{2}{6} = \frac{1}{3}$
 $D = \frac{2}{6} = \frac{1}{3} = \text{same as } C$
 $E = \frac{3}{6} = \frac{1}{2} = \text{same as } B$
 $F = \frac{3}{6} = \frac{1}{2} = \text{same as } B$
 $G = \frac{3}{6} = \frac{1}{2} = \text{same as } B$
 $H = \frac{4}{6} = \frac{2}{3} = \frac{8}{12} = \frac{12}{18} = \frac{16}{24} =$

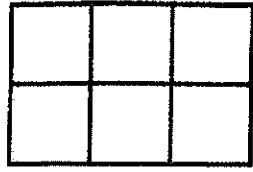
JJ

I multiplied by a form of one to get each fraction. I started by multiplying by $\frac{2}{2}$ then $\frac{3}{3}$ then $\frac{4}{4}$ then $\frac{5}{5}$ and finally $\frac{6}{6}$. For the first box, I counted the amount of squares in the rectangle, then I counted the shaded boxes. I got $\frac{1}{6}$ for the first example.

~~I did a sequence of multiplying fractions.~~

a. A small square is a square unit. What is the area of this rectangle? Explain.

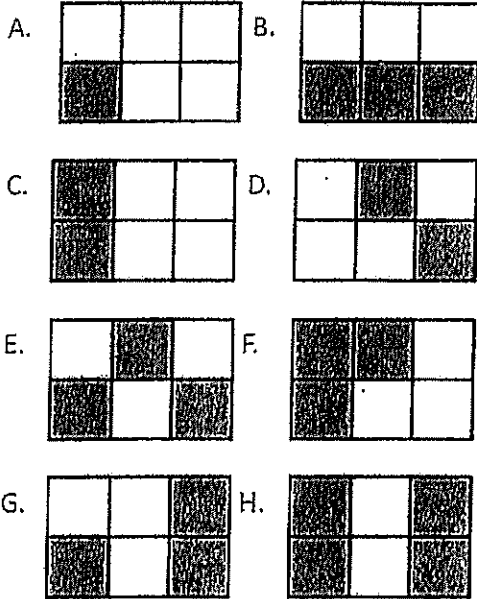
I think area of the rectangle is 6 square units. I know this because the rectangle



is split up into 6 small squares and it said that a small square is a square unit.

b. What fraction of the area of each rectangle is shaded blue? Name the fraction in as many ways as you can. Explain your answers.

- A. $\frac{1}{6}, \frac{2}{12}, \frac{4}{24}, \frac{3}{18}$
- B. $\frac{1}{2}, \frac{3}{6}, \frac{9}{18}, \frac{6}{12}$
- C. $\frac{1}{3}, \frac{2}{6}, \frac{4}{12}, \frac{6}{18}$
- D. $\frac{2}{6}, \frac{1}{3}, \frac{6}{18}, \frac{4}{12}$
- E. $\frac{1}{2}, \frac{3}{6}, \frac{50}{100}, \frac{9}{18}$
- F. $\frac{3}{6}, \frac{1}{2}, \frac{50}{100}, \frac{4}{8}$
- G. $\frac{1}{2}, \frac{3}{6}, \frac{500}{1000}, \frac{6}{12}$
- H. $\frac{4}{6}, \frac{8}{12}, \frac{12}{18}, \frac{16}{24}$



I think

To find the fraction of the shape, I looked at how many parts the rectangle was split into. That would be the denominator ($\frac{6}{6}$). Then I looked at how many parts was shaded, and that would be the numerator ($\frac{1}{6}$). To find the equivalent fraction I would double the numerator and denominator.

One way is to multiply by a form of one. ~~For example~~ Ex: $\frac{3}{6} \cdot \frac{3}{3} = \frac{9}{18}$

$\frac{3}{3}$ is a form of one. When you multiply by 1, the value stays the same.



Name: _____

EQUIVALENCY ARGUMENT

Find a fraction equivalent to $\frac{3}{8}$. Use diagrams, equations, and mathematical principles to prove that the fractions are equivalent.

Make sure your argument includes a claim, evidence, warrants, reasoning and conclusion.

Claim: The answer is $\frac{6}{16}$

Evidence:

$$\frac{3}{8} = \frac{6}{16} \text{ because}$$

and Reasoning

Warrant: $\frac{6}{16}$ is the right answer because if you times ~~it~~ ^{the fraction} by ~~7~~ (which is $\frac{2}{2}$) you get $\frac{6}{16}$ it is the same because the numerator and the denominator ~~is~~ ^{are} times by ~~1~~ ¹ ($\frac{2}{2}$) so it will be the same value. Any thing ~~th~~ ^{times} 1 is the same value

Conclusion: $\frac{6}{16}$ is equal to $\frac{3}{8}$ because $\frac{2}{2}$ is equal to 1 and anything times 1 is the same value so...

$$\frac{3}{8} \times \frac{2}{2} = \frac{6}{16}$$

so this why $\frac{3}{8}$ is equivalent to $\frac{6}{16}$

EQUIVALENCY ARGUMENT

Find a fraction equivalent to $\frac{3}{8}$. Use diagrams, equations, and mathematical principles to prove that the fractions are equivalent.

Make sure your argument includes a claim, evidence, warrants, reasoning and conclusion.

I believe that there is a fraction equivalent to $\frac{3}{8}$.

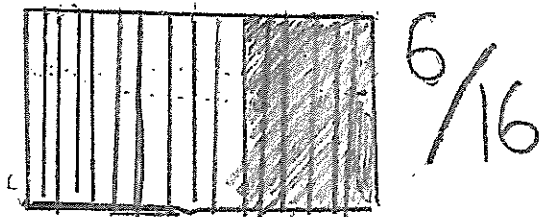
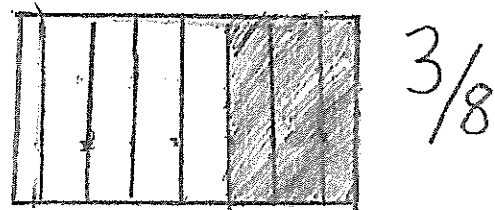
One possible equivalent fraction is $\frac{6}{16}$. This is proven by the equation and diagram below.

Equation

$$\frac{3}{8} \cdot \frac{2}{2} = \frac{6}{16}$$

This works because $\frac{2}{2}$ is equal to 1 or the giant 1. Also you are multiplying the numerator and denominator by the same thing.

Diagram



So as you can see, $\frac{3}{8}$ can easily be change to an equivalent fraction.

Name [REDACTED]

EQUIVALENCY ARGUMENT

Find a fraction equivalent to $\frac{3}{8}$. Use diagrams, equations, and mathematical principles to prove that the fractions are equivalent.

Make sure your argument includes a claim, evidence, warrants, reasoning and conclusion.

claim - $\frac{6}{16}$ it is just doubled

evidence - $3 \times 2 = 6$
 $8 \times 2 = 16$ not a hole they are
 both not holes

warrants - $\frac{3}{8} \times \frac{2}{2} = \frac{6}{16}$

conclusion / reasoning - The numbers are just doubled and are not hole.